

Ionization structure and a critical visual extinction for turbulent supported clumps

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Abstract. We show that the fractional ionization in a wide range of models of cloud chemistry undergoes a steep decline at extinctions of $A_V \simeq 2 - 3$. We identify this extinction with the critical value for clumps in the Rosette Molecular Cloud: clumps with A_V above ~ 3 may contain embedded stars, while those with extinction below this value do not. We argue that the ionization decline at this critical extinction is directly related to the extent of turbulent support in the cloud. This leads us to investigate for the first time the chemical evolution of a cloud that is initially magnetically supported against collapse perpendicular to the field lines, but is collapsing along the field lines in a 1-D mode, up to an unknown but critical density. The fractional ionization corresponding to this critical density then allows ambipolar diffusion to control a collapse across the large-scale magnetic field as well as parallel to it. The results of the chemical evolution of a cloud undergoing this two-stage collapse are presented, and are shown to be sensitive tracers of the details of the collapse mode.

Key words: molecular processes – stars: formation – ISM: abundances; clouds; magnetic fields; molecules

1. Introduction

In their work on the clumpy structure of the Rosette Molecular Cloud (RMC), Williams, Blitz and Stark (1995) identified seven star forming clumps, none of which has an estimated ^{13}CO column density, $N(^{13}\text{CO})$, of less than 10^{16} cm^{-2} . From their Fig. 21, it appears that eight or nine other clumps have $N(^{13}\text{CO}) > 10^{16} \text{ cm}^{-2}$ but contain no stars. The estimated values of $N(^{13}\text{CO})$ for the star forming clumps, with one exception, vary by only a factor of about 2, and the estimated masses vary by a factor of about 7. While one could argue that the Williams et al. (1995) data point to the existence of a minimum *mass* required for star formation to occur in the RMC, we suggest that they indicate, at least as strongly, the existence of a minimum *column density*, $N(^{13}\text{CO}) \simeq 10^{16} \text{ cm}^{-2}$, for stars to be born.

Hartquist et al. (1993) suggested that there should be a maximum value of the visual extinction, A_V , of a clump supported

against gravitational collapse along its large-scale magnetic field by internal Alfvén waves thought to comprise clump turbulence (Arons & Max 1975; Caselli & Myers 1995; Mouschovias & Psaltis 1995). Their idea was that above this critical visual extinction the damping rate of waves by ion-neutral friction (Kulsrud & Pierce 1969) is too rapid for the waves to be maintained at sufficient amplitudes to support a clump. This damping rate of waves in which the ion-neutral motions are well-coupled declines with extinction because it increases as the inverse of the number density of ions, n_i , (and proportionally to the square of the frequency). The value of n_i itself decreases with visual extinction. Recent numerical simulations of wave behaviour in self-gravitating clumps show that nonlinear magnetohydrodynamic waves can, in fact, support such clumps against collapse (Gammie & Ostriker 1996). In view of its relevance to wave damping in clumps it is now particularly timely to return to the issue of the behaviour of $x_i \equiv n_i/n_H$ (where n_H is the number density of hydrogen nuclei) as a function of A_V .

The view taken by Hartquist et al. (1993) and by us in the current work, is, thus, that much of the molecular material in giant molecular clouds is translucent to radiation and that photoionization affects its fractional ionization, which in turn plays a role in determining the rate at which material collapses. Our view is one that has much in common with that adopted by McKee (1989) who argued that star formation regulates itself because the births of stars lead to the production of radiation which raises the fractional ionization in translucent material and, consequently, lowers the rate of ambipolar diffusion. There are differences between McKee's and our points of view. We stress the role of turbulent support of clumps like those identified by Williams et al. (1995) (see also Bertoldi & McKee 1992); these are much more tenuous objects than the magnetically subcritical dense cores in which turbulent support is likely to be much less important than the support provided by the large-scale magnetic field and in which the collapse timescale is established by ambipolar diffusion. Consequently, we feel that McKee's (1989) considerations are likely to be of more relevance to more evolved objects formed through the collapse of the sorts of clumps Williams, Blitz & Stark (1995) found in their CO studies. In this paper we do present results for the fractional ionization for a wide variety of conditions; so many of our ion-

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ization calculations are of direct relevance for the application of McKee's (1989) model to self-regulation of later stages of the formation of low-mass stars.

Another reason for returning to this issue is that in the last few years a revision of ideas about the fractional ionization in some molecular cloud environments has occurred. Pineau des Forêts et al. (1992) and Le Bourlot et al. (1993a) discovered, for a range of assumed H_3^+ dissociative recombination rate coefficients, a class of dark cloud gas phase chemical equilibrium solutions in which the H_3^+ abundance is much lower and x_i much higher than in the solutions of the previously known class. Shalabiea & Greenberg (1995) have studied the effects on the existence of solutions belonging to the two classes of the assumed gas phase elemental fractional abundances of sulphur, x_S , and low ionization potential metals, x_M , such as sodium and magnesium, and of the assumed nature of grain surface chemistry modifications to the dark cloud gas phase chemistry. Though Le Bourlot et al. (1993b) and Flower et al. (1994) gave the fractional abundance of C^+ , $x(C^+)$, relative to hydrogen nuclei as a function of A_V for one cloud model with an assumed radiation field like that of the typical interstellar background field, there has been no exploration of the simultaneous dependence of the fractional ionization x_i on A_V , n_H (the number density of hydrogen nuclei), x_S , x_{Si} and x_M . The results of Le Bourlot et al. (1993b) and of Flower et al. (1994) indicate a transition at translucent depths for a model cloud in which $n_H = 10^3 \text{ cm}^{-3}$ from a solution of the high ionization class to one of the low ionization class.

In Sect. 2 of this paper we report the results of such an exploration and identify a variety of situations under which $-d(\log x_i)/dA_V$ is large. In Sect. 3 we give results for the chemical evolution of a parcel of gas collapsing from $n_H = 10^3 \text{ cm}^{-3}$ with an initial A_V within the range in which $-d(\log x_i)/dA_V$ is large. In our description of the collapse dynamics we include a plane parallel collapse phase, representing collapse along the field lines, followed by a phase during which the collapse takes place both across and along the large scale magnetic field and is regulated by ambipolar diffusion, the rate of which depends on the fractional ionization which is taken from our calculations.

2. Fractional ionization as a function of A_V , n_H , x_S , x_{Si} and x_M .

Fig. 1 contains the results of steady state equilibrium chemical models for x_i as a function of A_V , the visual extinction to the near edge of a semi-infinite plane-parallel cloud. Equilibrium results were obtained through the integration of rate equations from a time when all elements more massive than hydrogen were primarily in neutral and ionic atomic form but most of the hydrogen was in H_2 . The standard interstellar radiation background was assumed to be incident on the near side of the cloud, and it is assumed that a cosmic ray induced radiation field is present throughout the cloud (Prasad & Tarafdar 1983). In addition to an extensive network of gas phase reactions for which rate coefficients were taken primarily from the UMIST compilation (Millar et al. 1997), we included modifications to

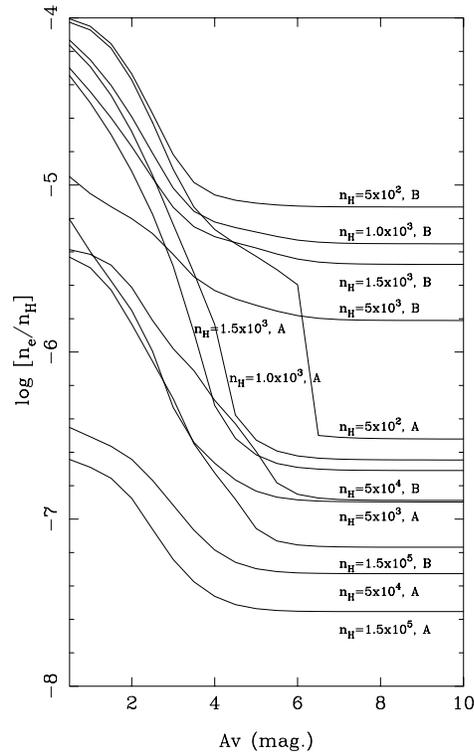


Fig. 1. Steady state fractional ionization as a function of A_V , n_H , x_S , x_{Si} , x_M

the gas phase chemistry due to the presence of grains by assuming that all material striking grains is immediately returned to the gas phase, but that many of the species are processed in such a way that much of the material is returned in the form of saturated species like H_2 , NH_3 , H_2S and CH_4 . The detection of NH in interstellar clouds (Meyer & Roth 1991; Crawford & Williams 1997) supports this view, at least for clouds with values of $A_V \sim 1$ (see Williams 1993). The rate at which particles of neutral species X were assumed to strike grain surfaces is $3.5 \times 10^{-18} \text{ s}^{-1} (m_X/\text{amu})^{-1/2} (n_H/\text{cm}^{-3})$, where n_H is the number density of hydrogen nuclei; charged particles were assumed to strike grains (mostly negatively charged) at a rate that is 18 times larger (following Rawlings et al 1992). All ions striking grains were assumed to return to the gas phase as neutral atoms and molecules. The cosmic ray ionization rate was taken to be $1.3 \times 10^{-17} \text{ s}^{-1}$. Molecular hydrogen is self-shielding, and CO was assumed to be sufficiently self-shielded and shielded by H_2 that only photons produced as a consequence of cosmic ray induced ionization are important for its photodissociation.

The results in Fig. 1 are for the two sets of assumed gas phase elemental abundances given in Table 1 (see Shalabiea & Greenberg 1995). Set A is similar to that required in many cases to reproduce chemical abundances measured for dark cores while Set B, which has higher fractional abundances of low ionization potential elements, is selected because diffuse clouds have much higher gas phase fractional abundances of those species than dark cores. The issue of the mechanisms that control the depletion of the low ionization elements is unclear at present

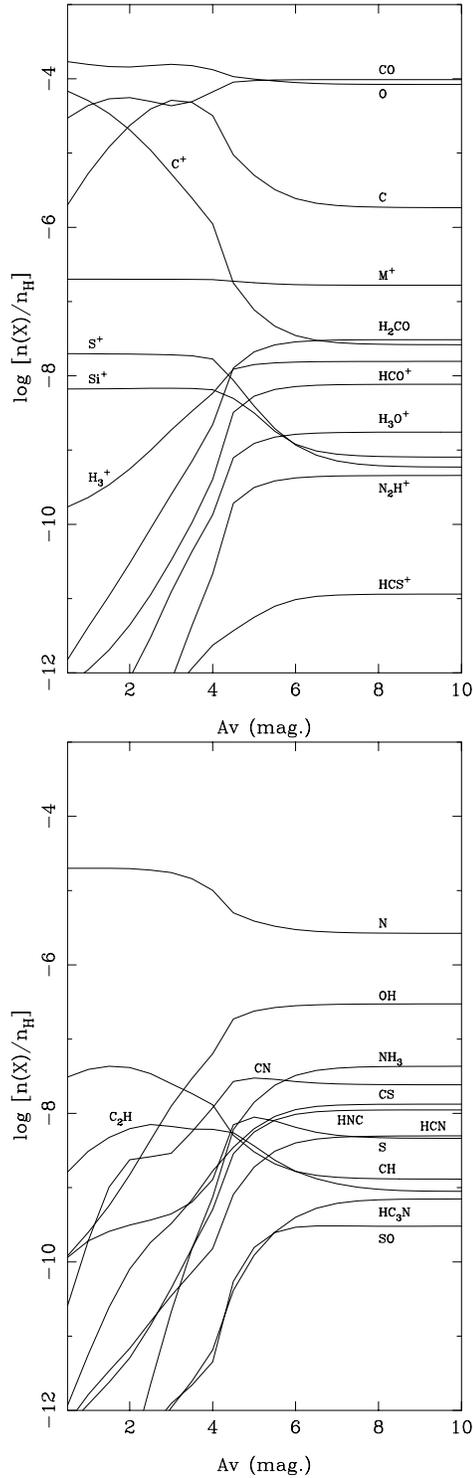


Fig. 2. Steady state fractional abundances of species as functions of A_V for $n_H = 10^3 \text{ cm}^{-3}$ and case A depletions (see text for description)

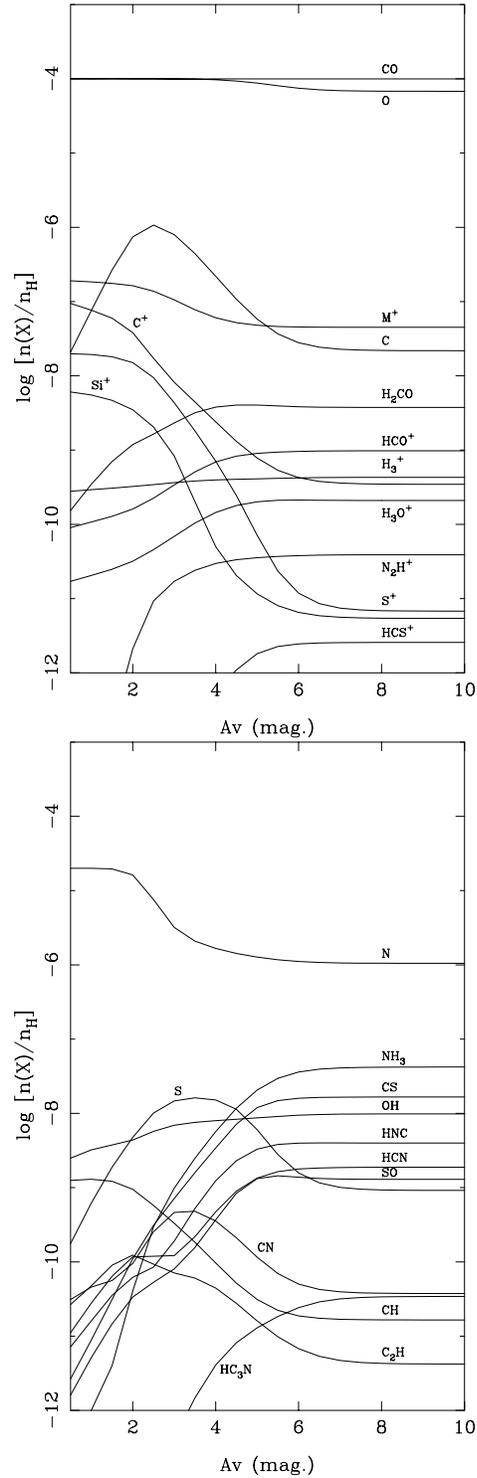


Fig. 3. Steady state fractional abundances of species as functions of A_V for $n_H = 5 \times 10^4 \text{ cm}^{-3}$ and case A depletions (see text for description)

(hence the parametrised approach adopted here), but is one of major importance for the chemistry of star formation, as the results in this paper indicate.

Inspection of Fig. 1 shows that for $n_H = 5 \times 10^2 \text{ cm}^{-3}$ (typical of the RMC clumps) the gradient $-d(\log x_i)/dA_V$ reaches a

maximum in the range $A_V \approx 2 - 3$ for Set B depletions and a local maximum for the same range of A_V for Set A depletions. For Set A depletions and $n_H = 500 \text{ cm}^{-3}$ a much higher value of $-d(\log x_i)/dA_V$ exists for a very small range of high values of A_V where a chemical phase transition occurs, but the high value

Table 1. Fractional elemental abundances relative to n_{H}

	A	B
	“dark”	“diffuse”
He	7×10^{-2}	7×10^{-2}
C	1×10^{-4}	1×10^{-4}
N	2×10^{-5}	2×10^{-5}
O	2×10^{-4}	2×10^{-4}
S	2×10^{-8}	3×10^{-6}
Si	7×10^{-9}	1×10^{-6}
M	2×10^{-7}	1×10^{-6}

of $-d(\log x_i)/dA_V$ in the range of $A_V \approx 2 - 3$ Set A as well as Set B depletions, is no doubt important for the ion-neutral damping of turbulence supporting RMC-like clumps. Taking ($1 \times 10^{16} \text{ cm}^{-2}/2$) to be half the critical measured value of the ^{13}CO column density from the edge of an RMC clump to its centre, $n(^{13}\text{CO})/n_{\text{H}} = 1 \times 10^{-6}$ (Williams et al. 1995), and the standard conversion of the hydrogen nuclei column density to A_V (Savage & Mathis 1979), we find that the critical visual extinction from the centre of an RMC clump to its edge is 2.5, in agreement with the regime of maximum $-d(\log x_i)/dA_V$ for $n_{\text{H}} = 500 \text{ cm}^{-3}$ identified in our calculations.

Results for x_i are also given in Fig. 1 for a range of values of n_{H} . As stated above, the ion-neutral damping rate of a wave of sufficiently low frequency is proportional to the square of the wave frequency divided by n_i . A comparison of the Set A graphs for $n_{\text{H}} = 5 \times 10^2 \text{ cm}^{-3}$ and $n_{\text{H}} = 5 \times 10^4 \text{ cm}^{-3}$ shows that at $A_V = 3$, the values of n_i for the two model clumps are roughly equal. Therefore the ion-neutral wave damping rate for a given frequency has roughly the same functional dependence on A_V , implying that even for dense cores the A_V dependence of x_i must be taken into account in any consideration of wave propagation.

The chemical calculation yielding x_i also provides information about the depth dependence of many other chemical abundances. Figs. 2 and 3 give results for the fractional abundances of a number of species for a $n_{\text{H}} = 1 \times 10^3 \text{ cm}^{-3}$, Set A clump and a $n_{\text{H}} = 5 \times 10^4 \text{ cm}^{-3}$, Set A dense core. The model results indicate that other than CO emissions only CH and OH emissions are likely to be detectable towards RMC clumps with $n_{\text{H}} = 1000 \text{ cm}^{-3}$, and also that the CH, OH and CO fractional abundances are not sensitive to x_{S} , x_{Si} and x_{M} . Unfortunately, values of CH and OH abundances are difficult to infer observationally. A comparison of Fig. 3 with Fig. 2 shows that M^+ is the dominant ion throughout a dense core, while C^+ is the dominant ion over a large range of A_V in $n_{\text{H}} = 1000 \text{ cm}^{-3}$ gas. Unlike RMC-type clumps with $A_V = 3$, a dense core with $A_V = 3$ and $n_{\text{H}} = 5 \times 10^4 \text{ cm}^{-3}$ is likely to produce observable emissions in a number of molecular species other than CH, OH and CO, including HCO^+ , N_2H^+ , H_2CO , CN, NH_3 , CS and possibly HNC and HCN.

Though our results are more extensive than those of previous authors, they are in harmony with those of Le Boulrot et al. (1993b), Flower et al. (1994), and Shalabiea & Greenberg (1995) in regions where comparisons can be made.

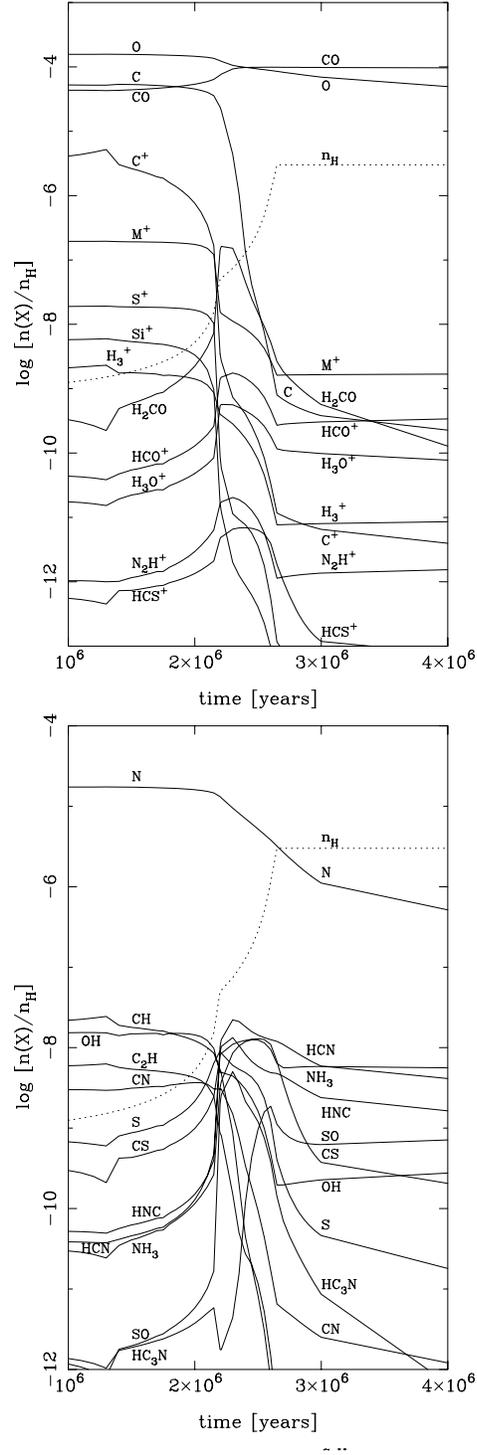


Fig. 4. Fractional abundances as functions of time since the onset of collapse for model 1 ($n_{\text{Hc}} = 2 \times 10^4 \text{ cm}^{-3}$). The dashed curves give ($n_{\text{H}}/10^{12} \text{ cm}^{-3}$)

3. Collapse from $A_V = 3$

We propose that $A_V \approx 2.5$ to 3.0 represents a critical range for the stability of RMC-type clumps. Above this critical range, the level of ionization and hence the level of turbulent support both fall. We do not know what mechanism is most effective

Table 2. Fractional abundances as functions of n_{H} for two collapse models

n_{H} (cm^{-3})	2×10^4	7×10^4	2×10^5	5×10^5
t_1 (10^6yr)	2.15	2.30	2.45	2.55
t_2 (10^6yr)	2.15	2.21	2.60	2.75
x_1 (CO)	6.399(-05)	9.277(-05)	9.830(-05)	9.875(-05)
x_2 (CO)	6.399(-05)	7.661(-05)	9.963(-05)	9.948(-05)
x_1 (CH)	8.577(-09)	8.711(-10)	1.919(-11)	3.025(-12)
x_2 (CH)	8.577(-09)	5.538(-09)	4.828(-12)	7.387(-13)
x_1 (OH)	9.808(-09)	4.442(-09)	2.322(-09)	9.937(-10)
x_2 (OH)	9.808(-09)	5.144(-09)	2.105(-09)	1.049(-09)
x_1 (CN)	3.077(-09)	1.504(-09)	1.816(-10)	4.394(-11)
x_2 (CN)	3.077(-09)	1.928(-09)	4.441(-11)	1.923(-11)
x_1 (CS)	2.456(-09)	1.101(-08)	1.271(-08)	1.261(-08)
x_2 (CS)	2.456(-09)	3.813(-09)	9.366(-09)	1.088(-08)
x_1 (SO)	5.854(-12)	4.404(-12)	4.399(-10)	1.587(-09)
x_2 (SO)	5.854(-12)	4.987(-12)	1.538(-09)	2.303(-09)
x_1 (C ₂ H)	2.510(-09)	1.523(-10)	2.020(-11)	5.211(-12)
x_2 (C ₂ H)	2.510(-09)	1.118(-09)	3.554(-12)	6.780(-13)
x_1 (H ₂ CO)	7.316(-09)	1.519(-07)	2.498(-08)	9.245(-09)
x_2 (H ₂ CO)	7.316(-09)	1.743(-08)	3.120(-09)	1.437(-09)
x_1 (HNC)	4.001(-10)	1.335(-08)	6.744(-09)	5.262(-09)
x_2 (HNC)	4.001(-10)	1.039(-09)	4.060(-09)	4.159(-09)
x_1 (HCN)	4.762(-10)	2.218(-08)	1.585(-08)	1.332(-08)
x_2 (HCN)	4.762(-10)	2.020(-09)	1.067(-08)	1.057(-08)
x_1 (NH ₃)	2.646(-10)	8.574(-09)	1.253(-08)	1.148(-08)
x_2 (NH ₃)	2.646(-10)	4.505(-10)	1.042(-08)	1.145(-08)
x_1 (HC ₃ N)	1.668(-11)	5.036(-09)	1.631(-09)	7.510(-10)
x_2 (HC ₃ N)	1.668(-11)	4.723(-11)	5.500(-11)	3.724(-11)
x_1 (M ⁺)	1.212(-07)	4.376(-08)	6.948(-09)	4.368(-09)
x_2 (M ⁺)	1.212(-07)	1.366(-08)	9.742(-09)	7.768(-09)
x_1 (C ⁺)	1.681(-07)	7.368(-10)	2.645(-10)	8.348(-11)
x_2 (C ⁺)	1.681(-07)	2.786(-08)	3.048(-10)	8.494(-11)
x_1 (S ⁺)	1.035(-08)	1.144(-11)	5.705(-12)	1.764(-12)
x_2 (S ⁺)	1.035(-08)	2.649(-09)	2.931(-11)	3.127(-12)
x_1 (i)	3.095(-07)	1.480(-08)	9.122(-09)	5.345(-09)
x_2 (i)	3.095(-07)	7.790(-08)	8.915(-09)	5.330(-09)

Note that the chemically driven desorption of unsaturated species are here assumed to eject *all* molecules arriving at grain surfaces (see Williams & Taylor 1996), so that the abundances in Figs. 4 and 5 are not constrained by freeze-out. Consequently, the late-time peaks in hydrocarbons and related species (Ruffle

et al. 1997) are not evident. In fact, the results in Figs. 4 and 5 are similar in character to those of Howe et al. (1996) who showed that reasonable fits to the chemistry in cores A-D of TMC-1 could be obtained if a low effective freeze-out rate is assumed.

In Table 2, the calculated fractional abundances when the collapse has attained a density of $n_{\text{H}} = 2 \times 10^4 \text{ cm}^{-3}$ of all species are the same for both models. At this point the two models have yet to diverge. After this point, the fractional ionization in model 1, in which the plane-parallel collapse at constant A_{V} occurs until $n_{\text{Hc}} = 2 \times 10^4 \text{ cm}^{-3}$, is lower than in model 2 where $n_{\text{Hc}} = 6 \times 10^4 \text{ cm}^{-3}$. This is a consequence of the visual extinction being lower in model 2, leading to the background interstellar photons continuing to be important for longer than in the model 1. This leads to a suppression by photodissociation of the early-time peaks of some species in model 2, which do exhibit an early-time peak in model 1. In addition, greater amounts of C, C⁺ and O⁺ occur in model 2 than in model 1 at $n_{\text{H}} = 7 \times 10^4 \text{ cm}^{-3}$. However, one may account for the timescale difference between the two models, in that model 2 reaches the density of $n_{\text{H}} = 7 \times 10^4 \text{ cm}^{-3}$ earlier than model 1 and then reaches the following displayed density of $n_{\text{H}} = 2 \times 10^5 \text{ cm}^{-3}$ at a later time than model 1.

The late-time abundances of early-time species are reduced in model 2, as a result of the lower visual extinction at $n_{\text{H}} = 2 \times 10^5 \text{ cm}^{-3}$, and the longer time that model 2 takes to reach that density. However, NH₃, SO and CS are seen to still be increasing in abundance in model 2, whilst in model 1 their abundances have already peaked.

Recently Ruffle et al. (1997) have argued that the abundances of HC₃N and C₂H will rise at late times in dense cores as depletion occurs; Caselli et al. (1998) have even used the measured fractional abundances of HC₃N in numerous cores to infer the depletions, relative to solar abundances, of C, N and O on the assumption that they did not vary from element to element. Ultimately to establish reliably that depletion is usually the cause of high abundances of such putative early-time molecules, considerable data about the abundances of species with abundances that are sensitive to the relative depletions of trace elements must be gathered. Our current results show that for cores in which high fractional abundances of HC₃N and C₂H exist but are not due to high depletions, the ratio of the abundances of those two species will be significant for the inference of how A_{V} varied with n_{H} during collapse. In their work, Caselli et al. (1998) drew on published results for HC₃N in many cores; at the time of the submission of the present paper a comparably large set of data for C₂H do not exist in the literature.

4. Conclusions

The sharp decline in fractional ionization at $A_{\text{V}} \simeq 2 - 3$ is here associated with the distinction between starless and star-containing cores in the RMC, through changes in turbulent support. This concept has led us to perform a preliminary study of the chemical evolution of a collapsing cloud, in which the cloud can first collapse only along the magnetic field lines. As the col-

lapse proceeds, the fractional ionization declines until a multi-dimensional collapse modulated by ambipolar diffusion ensues. We show that while the details of the chemistry are broadly similar to other comparable studies that have much cruder models of collapse, the specific nature of the collapse - in particular, the density at which multidimensional collapse becomes significant - should be indicated by chemical abundances.

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