

Hubble constant from sosie galaxies and HIPPARCOS geometrical calibration

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Abstract. New distances, larger than previous ones, have been obtained for M 31 and M 81 based on the geometrical zero-point of the Cepheid Period-luminosity relation provided by the HIPPARCOS satellite. By combining them with independent determinations we define reasonable ranges for the distances of these important calibrating galaxies.

On this basis, we determine the Hubble constant from the method of sosies (look-alike) galaxies, galaxies having the same characteristics than the calibrators. The method is quite secure because it is purely differential and it does not depend on any assumption (apart from the natural one that two sosies galaxies have similar absolute luminosities). Nevertheless, the Malmquist bias has to be taken into account. The observations behave exactly as predicted from the analytical formulation of the bias. Thus, rejecting galaxies which are affected by the Malmquist bias we derive the Hubble constant:

$$H_o = 60 \pm 10(\text{external}) \text{km.s}^{-1} . \text{Mpc}^{-1}$$

If we strictly use the calibration obtained with HIPPARCOS and if the bias found in the Period-Luminosity Relation is considered, the Hubble constant is smaller than this ($\approx 55 \text{km.s}^{-1} . \text{Mpc}^{-1}$). This gives arguments in favour of the long-distance scale. We briefly discuss possible improvements aiming at still reducing the uncertainty.

Key words: galaxies: distances and redshifts – galaxies: individual: M 31 – galaxies: individual: M 81 – distance scale

1. Introduction

From recent measurements with HIPPARCOS astrometric satellite we have obtained new distances for 17 nearby galaxies on the basis of Cepheid geometrical parallaxes (Paturel et al., 1997). This provides us with a new calibration of the extragalactic distance scale. It would be interesting to look for the Hubble

constant derived directly from these calibrating galaxies. Unfortunately, their radial velocities are dominated by the local velocity field and not by the cosmological velocity. Thus, they cannot be used directly, but can be used for the calibration of a long-range criterion, like the Tully-Fisher relation (Tully and Fisher, 1977).

The TF relation - relation between the 21-cm line width and the absolute magnitude - is thus far the best way to extend extragalactic distance measurements beyond the local universe where calibrators can be measured. The distance modulus derived from this relation can be written as:

$$\mu = B_T^c - a.\log V_M + b = B_T^c - a.\log(W/2\sin i) + b \quad (1)$$

where μ is the distance modulus, B_T^c is the apparent total magnitude corrected for inclination and galactic extinction, V_M is the maximum velocity rotation, W is the 21-cm line width corrected for instrumental effect and non circular velocity, a and b are two constants. This seems quite simple but some difficulties exist: All the corrections for inclination effects on both B_T^c and W depend on models which use the axis ratio R_{25} of the external isophotes and the morphological type code T of the considered galaxy. Further, it has been said that a and b also depend on T (Roberts, 1978; Rubin et al., 1985; Theureau et al., 1997) and it has been suggested that the linearity is not necessarily satisfied (Aaronson and Mould, 1983; Mould and Han, 1989). The use of the TF relation is plagued by these problems and the resulting distance scale may appear less convincing.

The second problem is related to a statistical bias (the so-called Malmquist bias). This bias can be understood as following. First of all, at large distances only the intrinsically brightest galaxies are seen because any sample is limited to a given apparent magnitude. In addition, the chance of finding galaxies over- or under-luminous (for their W) is higher in a large sample, i.e. at a large distance. These features are clearly illustrated by the Spaenhauer diagram (see Sandage, 1994), a diagram of absolute magnitude M versus radial velocity V (or distance).

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In summary, if one wants to produce a sufficiently convincing value for the Hubble constant three difficulties have to be solved:

- there must be a secure zero-point calibration
- one has to correct for inclination effects and morphological type dependence.
- we have to overcome statistical biases like the Malmquist bias.

The first item (zero-point) is very important and will be discussed in Sect. 2 in the light of new results obtained in studying the catalog of HIPPARCOS Cepheids. Then, the method of sosies-galaxies used to solve the second problem (corrections of secondary effects) is discussed in Sect. 3. The third item (Malmquist bias) is considered in Sect. 4. Finally, an application to sosie galaxies of M 31 and M 81 is made in Sect. 5 and the results are presented in Sect. 6.

2. Discussion of the distance scale calibration

From a general compilation of Cepheid measurements we derived distances for 17 galaxies using geometrical parallaxes of 10 galactic Cepheids provided by the HIPPARCOS satellite (Paturol et al., 1997). The result was obtained through a generalization of classical precepts.

Three important points should be emphasized:

- The equations were linear. Thus, they were used only on the range BVRI and only for relatively small extinction (because the ratio of total to differential extinction is assumed to be constant for a given effective wavelength).
- The distance modulus of a given galaxy was directly connected to the mean distance modulus $\bar{\mu}$ of the HIPPARCOS galactic Cepheid sample. Any change in $\bar{\mu}$ will affect the final result. The uncertainty on $\bar{\mu}$ is large ($\sigma(\bar{\mu}) \approx 0.2$) because it is based mainly on 10 calibrating Cepheids (those having the highest weights).
- Evidence is given that the Period-Luminosity relation (PL) is affected, at least in some galaxies, by a statistical bias (incompleteness bias, similar to the Malmquist bias).

The distance moduli found in this way were about 0.2 magnitude larger than those generally admitted. For instance, the distance modulus of Large Magellanic Cloud (LMC) was found to be $\mu(LMC) = 18.7$ (Feast and Catchpole, 1997; Paturol et al., 1997), while RR Lyrae stars give $\mu(LMC) = 18.3$ (Fernley et al., 1997), the SN1987 gives $\mu(LMC) = 18.4 - 18.6$ (Gould, 1995; Panagia et al., 1997). From independent studies on Cepheids, the distance moduli is found between 18.5 and 18.7 (Gieren et al., 1998; Gieren et al., 1993). Anyway, the distance modulus of LMC lies between 18.3 and 18.7. Our value is in favour of the large ones. In our first study (Paturol et al., 1997) the distance moduli for M 31 and M 81 were $\mu(M31) = 24.8$ and $\mu(M81) = 28.1$ without correction for the bias and $\mu(M31) = 24.9$ and $\mu(M81) = 28.2$, with a tentative correction. Our result was in favour of a long distance scale.

Stricto Sensu, our results are compatible with the generally admitted distance moduli but the uncertainty on the zero-point is still large (0.2).

A new study has been undergone by one of us (PL) to revisit the HIPPARCOS PL calibration after the release of the whole HIPPARCOS catalogue. Some important conclusions are drawn:

- The value of $\bar{\mu}$ obtained from HIPPARCOS parallaxes must be based on confirmed solitary Cepheids. We rejected binary stars in our original sample but many remaining ones may still be binaries. This point was already underlined by Szabados (1997) and confirmed by us. A part of this effect can be understood by the nearness of confirmed solitary Cepheids which makes them less sensitive to the Lutz and Kelker bias (1973). This does not change the practical conclusion: It is better to base our zero-point on nearby solitary Cepheids.
- Using all available solitary Cepheids from the HIPPARCOS mission we confirmed exactly the V-band PL relation of Gieren and Fouqué (1998) who give $\mu(LMC) = 18.4$. Then, adopting their I-band PL relation we applied the dereddening method of Madore and Freedman (1991) and derived $\mu(M31) = 24.6$ and $\mu(M81) = 27.6$, without correcting for the bias (i.e. with all periods).
- The incompleteness bias on the Cepheid PL relation has been independently confirmed using available HST observations and numerical simulations. It is generally small (less than 0.2 magnitude) because the dispersion of the PL relation is small. Nevertheless, correcting the bias (by constructing the growth curve $\mu = f(\log P)$) we derived $\mu(M31) = 24.7$ and $\mu(M81) = 27.7$.

In conclusion of this section, we will adopt $\mu(M31) = 24.6 \pm 0.2$ and $\mu(M81) = 27.6 \pm 0.2$ to derive the range of possible Hubble constant but we will keep in mind that our study with HIPPARCOS catalogue leads to distance moduli 0.1 mag larger after correction for incompleteness bias on the Cepheids Period-Luminosity relation.

Now we have to discuss a method to avoid uncertainties in the correction of secondary effects on the TF relation.

3. Overcoming secondary effects with sosies

We could make a model for correcting inclination effects and morphological type dependence. This necessarily leads to uncertainties because of the model dependency. The way we have chosen here is different. We will not try to correct for these perturbing effects but we will create a situation where the correcting terms disappear.

If one selects galaxies having very nearly the same morphological type, the same axis ratio and the same rotational velocity than a given calibrating galaxy (here, M 31 or M 81), they will have the same absolute magnitude as the calibrator. This is the direct consequence of Rel. 1. This approach (Paturol, 1981) is called the method of sosie galaxies ("sosies" is the French word for look-alike). Indeed, such galaxies will have the same appear-

ance and the same physical properties. The distance modulus of a sosie galaxy is simply obtained by the relation:

$$\mu = \mu(\text{calib}) + B_T^c - B_T^c(\text{calib}) \quad (2)$$

where "calib" refers to the considered calibrator (M 31 or M 81) and B_T^c is the apparent magnitude corrected for secondary effects. In this case, the corrections for inclination effects and morphological type dependence have no incidence of the final result because inclination and morphological type are the same. Nevertheless, a differential correction is required for the galactic extinction, but it is quite small because this is a differential secondary effect. This is still more valid because we restrict the selection to low extinction regions. Note that Sandage (1996) also made use of the concept of sosie galaxies by considering galaxies having the same morphological type and the same luminosity class.

4. Statistical bias

In our first application of the method of sosies (Paturel, 1981) we naively claimed that "this method is free from any Malmquist bias" because we thought that at a given rotational velocity only one single value of the absolute magnitude may exist. In fact, this is not correct. Sosie galaxies do have a dispersion of absolute magnitudes around a constant mean value. Making a magnitude limited sample selects the brightest galaxies of the distribution and then biases the sample.

The importance of the bias in connection with morphological luminosity classes was described as far back as 1975 (Sandage and Tamman, 1975; Teerikorpi, 1975a,b). Two diagrams help one to understand the bias. The *Plateau diagram* from which the method of the normalized distance is derived (Teerikorpi, 1984, Bottinelli et al., 1986) and the *Spaenhauer diagram* (Spaenhauer, 1978; Sandage, 1994). The connection between these diagrams has been recently reviewed by Teerikorpi (1997) who suggests the term *Malmquist bias of the second kind* for the distance dependent bias, to distinguish it from the classical Malmquist bias.

The Spaenhauer diagram shows how the absolute magnitude behaves as a function of the kinematical distance (i.e., distance estimated by the velocity). An illustration of this diagram is given in Fig. 1 for galaxies of a nominal absolute magnitude of -21 . The equation of the envelope of the distribution (dotted curves in Fig. 1) can be calculated as $|M' - M_o| = c \cdot \log V + d$, where $c = 2\sigma/1.57$ and where d is a function of the space density of considered galaxies (Paturel, 1998). σ is the dispersion of the TF relation for the given rotation velocity.

The Plateau diagram shows how $\log H$ changes with the kinematical distance. For galaxies assumed to have the same absolute magnitude (like the sosies of a given calibrator) the Plateau diagram exhibits a plateau where $\log H$ is unbiased (see Figs. 3 and 4). The method of the Normalized Distance consists in compressing or expanding the x -axis of the Plateau diagram according to the absolute magnitude so that the plateau becomes the same whatever the absolute magnitude of galaxies. This is achieved by multiplying the 'distance' V by $10^{0.2M}$. Because M

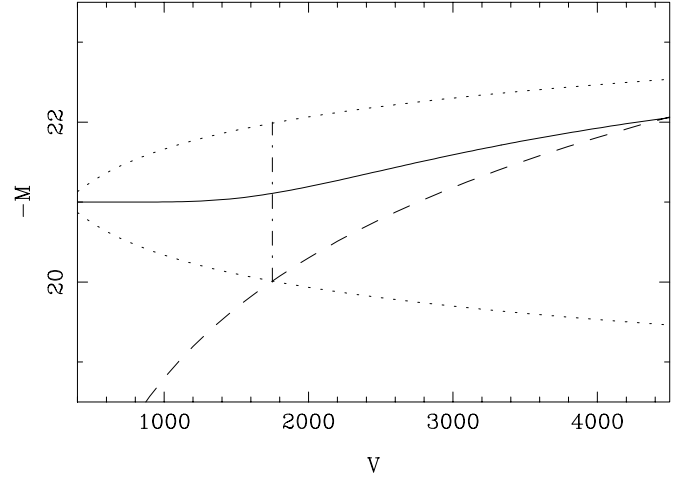


Fig. 1. Spaenhauer diagram: for a sample of galaxies, limited to an apparent magnitude and having on the mean the same absolute magnitude only galaxies above the completeness limit are visible (dashed curve). The dispersion around the mean increases with the size of the sample (i.e. with the distance) but reaches a physical limit as shown by the envelopes (dotted curves). The actual mean apparent absolute magnitude will follow the solid line. The vertical line shows where the bias begins.

is not known *a priori* it can be replaced through the relation by $10^{a/5(\log V_M)}$, where a is the slope of the Tully-Fisher relation.

¹ The thus corrected distance is called the normalized distance. An example of the normalized diagram is given in Fig. 5.

The analytical curve for the Malmquist bias of the 2nd kind (Teerikorpi, 1975b) allows one to predict the change of the mean absolute magnitude $\Delta M = M' - M_o$ (or the change $\Delta \log H = \log H' - \log H_o$) with the 'distance' (V). M' and $\log H'$ refer to biased quantities. We have:

$$\Delta M = M' - M_o = \sigma \sqrt{\frac{2}{\pi}} \frac{e^{-A^2}}{1 + \text{erf}(A)} \quad (3)$$

with

$$A = \frac{M_{lim} - M_o}{\sigma \sqrt{2}} \quad (4)$$

and

$$\text{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt \quad (5)$$

and

$$M_{lim} = m_{lim} - 25 - 5 \log V / H_o \quad (6)$$

The bias curve in the Plateau diagram is simply:

$$\Delta \log H = \log H' - \log H_o = -0.2 \Delta M \quad (7)$$

The completeness limit curve (dashed curve in our diagrams) will show where the sample is cut. No galaxies will

¹ In the case of sosie galaxies we will use the absolute magnitude $M(\text{calib})$ of the calibrator to perform the normalization

Table 1. Parameters of Calibrating Galaxies

parameter	M 31	M 81
μ	24.6 ± 0.2	27.6 ± 0.2
M_B	-21.49	-20.62
T_{code}	3.0 ± 0.3	2.5 ± 0.6
$\log R_{25}$	0.48 ± 0.05	0.31 ± 0.07
B_T^c	3.11 ± 0.4	6.98 ± 0.32
$\log V_M$	2.397 ± 0.010	2.338 ± 0.022

appear below this limit for the considered absolute magnitude. In the Spaenhauer diagram the completeness limit is given by Eq. 6. This curve is unique whatever the absolute magnitude (the equation does not depends on M_o). In the Plateau diagram the limit can be deduced from:

$$\log H_{lim} = 0.2M_o + 5 - 0.2m_{lim} + \log V \quad (8)$$

In the Plateau diagram it is obvious that there is a completeness limit for each calibrator because $\log H_{lim}$ explicitly depends on M_o . When the normalization is applied on x -axis multiplying by $10^{0.2M_o}$, the completeness limit becomes unique for each M_o .

5. Application to M 31 and M 81 sosie galaxies

5.1. The sample

In the present paper we use only the calibrators M 31 and M 81 because they are the brightest ones. The main characteristics of these galaxies are given in Table 1. All observed astrophysical parameters are taken from the LEDA database which is freely accessible². Distance moduli are taken according to the discussion of Sect. 2 and the absolute magnitudes are derived from them using the corrected apparent magnitudes. Note that the correction for galactic extinction on magnitudes are taken following the RC2 system (de Vaucouleurs et al., 1976). The essential difference with the Burstein-Heiles model occurs near the galactic poles (see Paturel et al., 1997) where the extinction is assumed to be 0.2 magnitudes. However, this has no influence on the present results because the constant term is cancelled in our differential method.

Using the LEDA database we selected sosie galaxies, i.e. galaxies having nearly the same morphological type code (T), the same \log of axis ratio ($\log R_{25}$) and the same rotational velocity ($\log V_M$), as M 31 or M 81. Further, we selected only galaxies with accurate apparent magnitude ($\sigma(B_T) \leq 0.4$) and rotational velocity ($\sigma(\log V_M) \leq 0.08$) and no discrepancies in observed radial velocity. The tolerances are chosen to equal a typical error in each parameter. They are ± 1.5 for the morphological type code, ± 0.12 for $\log R_{25}$ and ± 0.08 for $\log V_M$.

Using such criteria we obtained a sample of 43 sosies of M 31 and 119 sosies of M 81. For each galaxy the following parameters are known (they all conform to the description given by Paturel et al., 1997):

² **telnet:** telnet leda.univ-lyon1.fr, login: leda
or **world-wide-web:** http://www-obs.univ-lyon1.fr/leda

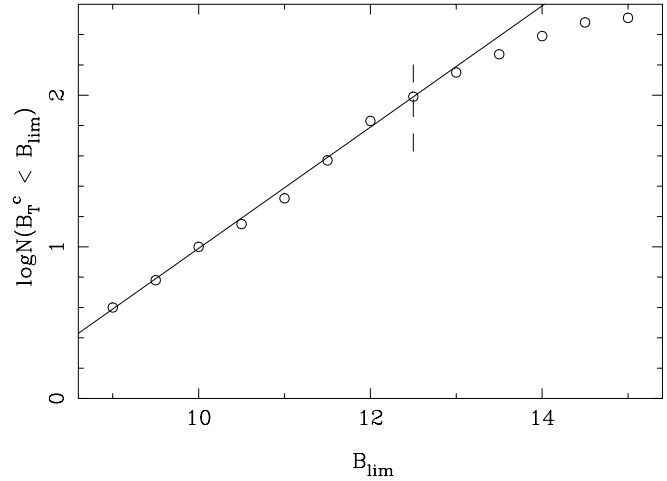


Fig. 2. Completeness curve of the sample. This curve is used to define the apparent limiting magnitude of our sample in an objective manner. The completeness is fulfilled up to an apparent magnitude of $B_{lim} \approx 12.5$ (vertical line).

- Column 1: PGC name according to Paturel et al. (1989a,b)
- Column 2: Right ascension and Declination for 2000 in (h,mn,s) and (deg,arcmin,arcsec) respectively.
- Column 3: Corrected total B_T^c magnitude in the RC3 system (de Vaucouleurs et al., 1991) - except for the galactic extinction.
- Column 4: Radial velocity corrected for the infall of the Local Group onto the Virgo cluster. The infall velocity is 170 km.s^{-1} according to Sandage and Tammann (1990), the position of the Virgo cluster is $SGL = 104 \text{ deg}$ and $SGBD = -2 \text{ deg}$, in supergalactic coordinates. This velocity is used as a relative kinematical distance.

As we saw in previous section, in order to use the Normalized Distance method it is compulsory to have a sharp apparent limiting magnitude in our sample. This magnitude limit and the resulting useful sample can be derived by constructing the curve $\log N$ vs. the apparent magnitude B_T^c (N is the cumulative number of galaxies with $B_T^c < B_{lim}$). The result must be a straight line. The magnitude at which the curve bends down gives the limiting magnitude B_{lim} . The slope should be $0.6 = 3/5$ if the distribution of galaxies is homogeneous ($N \propto r^3$). In practice, this value is rarely reached. The slope is always lower. In the local universe it has been shown that the slope is close to $0.4 = 2/5$ (Paturel et al., 1994). This is also consistent with a recent derivation of the radial space density by a method using the Tully-Fisher distance moduli (Teerikorpi et al., 1998).

For our sample the completeness curve $\log N$ vs B_T^c is built (Fig. 2) by combining sosies of both calibrators M 31 and M 81 (the apparent limiting magnitude is an observational limit which does not depend on the absolute magnitude of considered objects). The completeness is fulfilled up to an apparent magnitude of $B_{lim} \approx 12.5$. The slope is in agreement with our previous result (0.4).

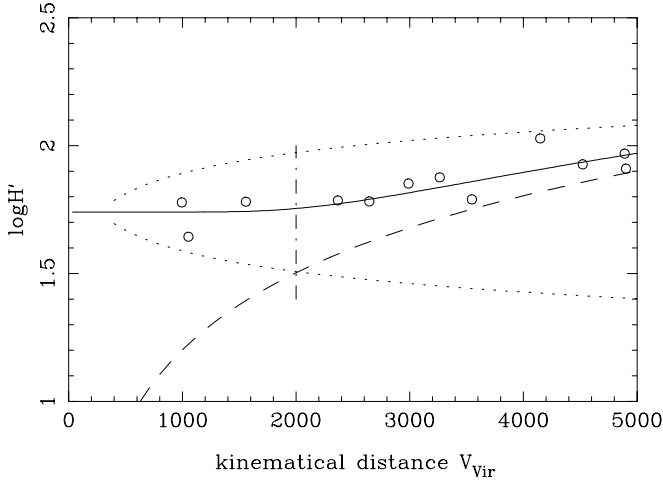


Fig. 3. The Plateau diagram ($\log H'$ vs. V_{vir}) for sosie galaxies of M 31. (the velocity is used as an estimator of relative distances). As expected, $\log H'$ increases with the distance because of the Malmquist bias. The full line represents the model of the bias from Teerikorpi (1975b). The dashed line represents the limit in apparent magnitude ($B_{lim} = 12.5$). The dotted curves represent the envelope of the distribution. The vertical line corresponds to the distance where the bias begins. The adopted H_o is $50 \text{ km.s}^{-1} . \text{Mpc}^{-1}$.

Thus, the diagrams will be made using only galaxies brighter than $B_T^c = 12.5$. The corresponding sample is given in Appendix A.

5.2. Construction of the Plateau diagram

The Hubble constant is calculated from the relation:

$$\log H' = \log V_{vir} - 0.2[\mu(\text{calib}) + B_T^c - B_T^c(\text{calib}) - 25] \quad (9)$$

for each galaxy for which $V_{vir} \geq 500 \text{ km.s}^{-1}$ (with this radial velocity limit we avoid the effect of random peculiar velocities). Figs. 3 and 4 show the Plateau diagrams, $\log H'$ vs. V_{vir} , for M 31 and M 81 respectively. The bias curve (Eq. 7) is calculated using $B_{lim} = 12.5$ (previous section) and $\sigma = 0.7 \text{ mag}$ (Fouqué et al., 1990). The expected increase of $\log H'$ is clearly visible. It reveals the presence of a Malmquist bias. The velocity at which the bias becomes significant (i.e. $\Delta M \approx 0.05$) is 2000 km.s^{-1} for M 31 and 1400 km.s^{-1} for M 81.

For sosie galaxies of a given calibrator, the Plateau diagram has the same meaning than the Spaenhauer diagram. The deviation of $\log H'$ simply reflects the corresponding deviation of M' in the Spaenhauer diagram.

We can draw the Normalized distance diagram by superimposing both Plateau diagrams after having expanded the x -axis for M 81 by the factor $10^{-0.2(M_o(M31) - M_o(M81))}$, i.e. 1.49. Note that in this case we adopted a mean Hubble constant $H_o = 60 \text{ km.s}^{-1} . \text{Mpc}^{-1}$. The result is given in Fig. 5. From this diagram it appears that the bias begins near a normalized 'distance' of $V_{vir} = 2000 \text{ km.s}^{-1}$ (i.e., 1.49×1400) This will limit the unbiased sample to only 9 galaxies which will be used to define the most likely value of the Hubble constant H_o .

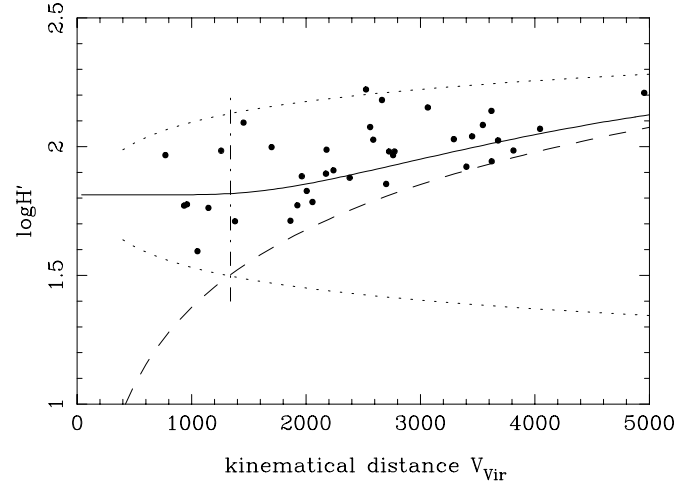


Fig. 4. The Plateau diagram for sosie galaxies of M 81. (same comments as the previous figure). The adopted H_o is $65 \text{ km.s}^{-1} . \text{Mpc}^{-1}$.

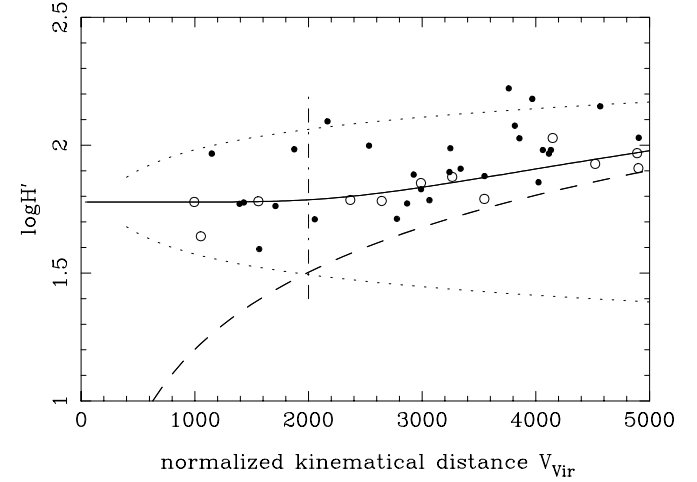


Fig. 5. The Normalized distance ($\log H'$ vs. $V_{vir} 10^{-0.2(\Delta M_o)}$) for sosie galaxies of both M 31 and M 81 (see text for the calculation of the normalization factor). The mean H_o adopted is $60 \text{ km.s}^{-1} . \text{Mpc}^{-1}$.

5.3. Mean Hubble constant derived from the geometrical zero-point

The final sample of unbiased galaxies is given in Table 2. It is rather small as expected from the size of the sosies sample and from the restriction $V_{vir} \geq 500 \text{ km.s}^{-1}$.

From the mean $\log H_o = 1.78 \pm 0.04$ we derive the Hubble constant $H_o = 60 \pm 5(\text{internal}) \text{ km.s}^{-1} . \text{Mpc}^{-1}$. If we are using the extreme values for μ_{calib} we find that the Hubble constant lies between 47 and $65 \text{ km.s}^{-1} . \text{Mpc}^{-1}$.

6. Conclusion

A reasonable value of the unbiased Hubble constant would be:

$$H_o = 60 \pm 10(\text{external}) \text{ km.s}^{-1} . \text{Mpc}^{-1} \quad (10)$$

Table 2. Sample of unbiased galaxies

M 31 sosies	B_T^c	V_{Vir}	$\log H_o$
PGC14638	9.61	995	1.778
PGC39724	10.40	1053	1.644
PGC51233	10.57	1559	1.781
M 81 sosies	B_T^c	V_{Vir}	$\log H_o$
PGC00218	10.87	1147	1.762
PGC10208	10.41	960	1.776
PGC33550	8.98	771	1.967
PGC35164	10.38	935	1.771
PGC37306	9.96	1258	1.984
PGC43798	11.52	1051	1.594
mean			1.78 ± 0.04

Nevertheless, we believe that the correct value is more probably near the lower limit because we have demonstrated that the PL relation of Cepheids also suffers from a statistical bias.

It is clear, that the bias appears already at a short distance, even when a luminous galaxy is used as calibrator. Hence, it is difficult to obtain a secure Hubble constant from low luminosity galaxies. Indeed, then restricting the sample to the unbiased plateau requires a cut at a very low radial velocity, just where random velocities start to dominate. This justifies that we used first M 31 and M 81 as calibrators. However, one should ask whether these galaxies have an absolute magnitude representative of their rotation velocity. The positions of M 31 and M 81 in a TF diagram are quite normal (see for instance Fouqué et al., 1990), which supports that they are good calibrators.

The positive sides of the sosies method make it necessary to enlarge the sample in the future. This can be achieved only by using deeper samples which require more HI measurements. Besides, weaker sosies criteria which require that galaxies have the same morphological type and the same axis ratio, but not necessarily the same 21-cm line width W as a calibrator will greatly improve the accuracy of the TF relation because inclination and morphological type effects will be cancelled.

Another way to improve the result may come from infrared photometry. Indeed, even with the method of sosie galaxies it is necessary to correct for galactic extinction. Obviously, only the difference between the extinctions in front of the sosies galaxy and the calibrator enter the final result. Nevertheless, it is still a part of the uncertainty.

In view of this promising aspects, we are engaged in a program aiming at collecting deeper samples of sosie galaxies especially in the infrared domain.

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Appendix A: samples of M 31 and M 81 sosie galaxies brighter than $BTc=12.5$

PGC name	RA. (2000) DEC.	BTc	V(Vir)
M 31	004244.4+411608	3.11	-116
PGC05268	012519.7+340128	12.41	4902
PGC05344	012621.6+344214	12.22	5338
PGC10048	023912.2+105050	12.31	3547
PGC14638	041205.5-325228	9.61	995
PGC26157	091619.6-233804	11.45	2368
PGC36964	114950.1-384705	11.71	2644
PGC39724	121950.9+293654	10.40	1053
PGC51233	142020.5+035559	10.57	1559
PGC54001	150735.4+193457	12.11	4891
PGC55256	153007.8-383857	12.15	4522
PGC55740	153958.1+580457	11.70	3264
PGC62951	191443.8-621618	11.46	4148
PGC63214	192649.8-545704	11.63	2989
PGC63464	193842.8-294832	12.31	6011

PGC name	RA. (2000) DEC.	BTc	V(Vir)
M 81	095533.5+690400	6.98	201
PGC00218	000315.1+160845	10.87	1147
PGC03260	005507.9+313229	12.22	5606
PGC04777	011945.5+032437	11.87	2381
PGC07525	015920.3+190022	10.28	2524
PGC10208	024144.7+002631	10.41	960
PGC13059	033108.4-333744	10.54	1699
PGC13108	033203.1-204904	11.53	1379
PGC13179	033336.6-360817	9.73	1454
PGC13584	034157.2-044221	12.07	4045
PGC18355	060340.2-693541	12.09	3678
PGC23086	081414.4+212125	12.43	3401
PGC23362	081948.2+220138	12.46	3622
PGC24427	084135.0-201858	11.76	5555
PGC24464	084240.1+141710	12.02	2056
PGC24558	084430.1-202101	11.82	3291
PGC25097	085607.9-032139	11.94	1924
PGC28376	095115.8-324518	11.31	2587
PGC29591	101009.9-122602	11.71	3545
PGC29993	101619.3-333353	11.65	2725
PGC31335	103508.5-434132	10.60	2663
PGC31533	103715.6-413742	11.04	2560
PGC33550	110548.9-000215	8.98	771
PGC35164	112607.7+433506	10.38	935
PGC37306	115349.5+521939	9.96	1258
PGC39212	121533.7-353746	11.69	2773
PGC39656	121922.0+060601	12.17	1864
PGC43798	125329.1+021011	11.52	1051
PGC45170	130414.6-102021	11.05	3064
PGC46304	131743.4-320605	11.59	2174
PGC49359	135328.1+375452	12.36	3812
PGC49563	135616.8+471417	11.75	2006
PGC50031	140250.5+491025	11.59	2240
PGC51932	143205.2+575524	11.13	2179
PGC54364	151345.7-141615	11.42	1963

PGC62178	183833.7+252238	11.48	3620
PGC62528	185255.5-591520	11.87	3451
PGC64601	202334.0+062638	11.81	4955
PGC64884	203138.5-305001	11.75	2761
PGC67839	220102.0-131610	12.26	2700

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